

Effects of Out-of-Plane Ply Wrinkles on the Pre and Post-buckling Behavior of Carbon Fiber Reinforced Composites Using Finite Element Analysis

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September 2022



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Introduction



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Introduction

Composites and their applications:

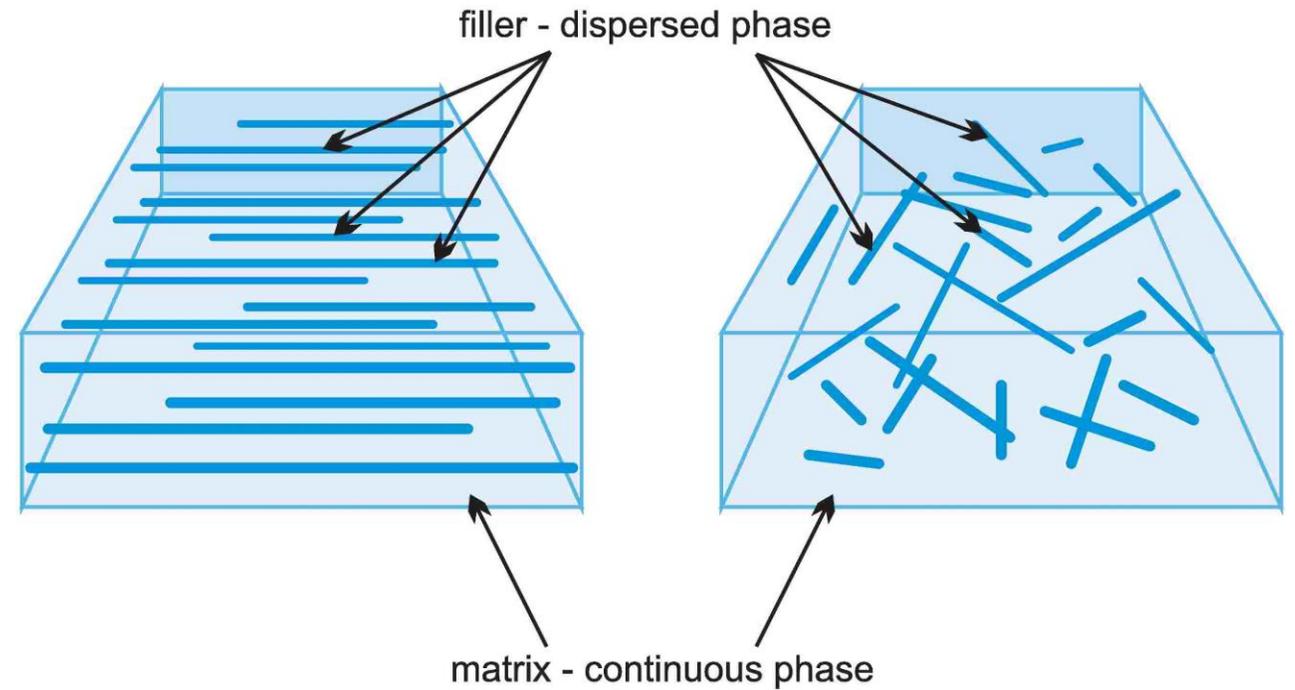
- ✓ Aerospace
- ✓ Automotive
- ✓ Civil



Introduction

Fiber reinforced composites:

- ✓ Polymer Matrix Composites
- ✓ Ceramic Matrix Composites
- ✓ Metal Matrix Composites



Introduction

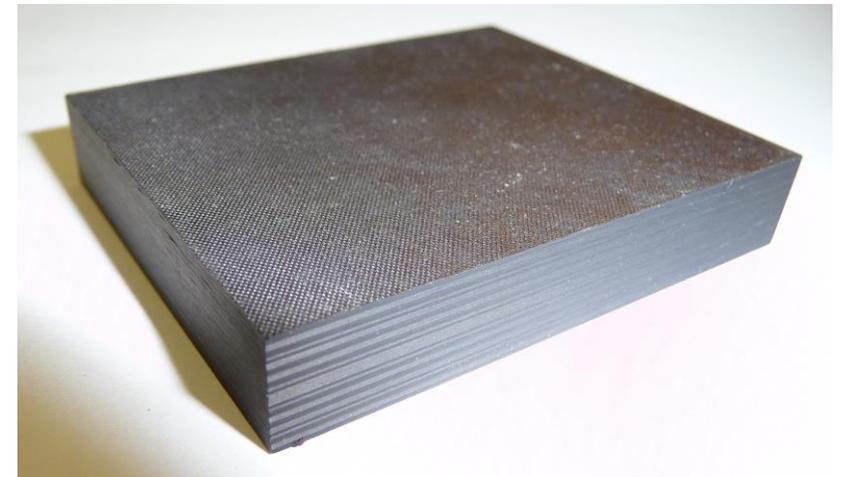
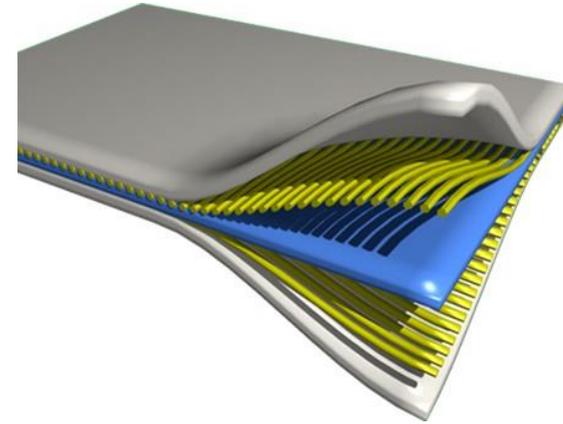
Carbon Fiber Reinforced Polymers (CFRP):

✓ Advantages:

- High Strength and Stiffness to Weight Ratio
- Attractive Appearance (in sport cars)

✓ Disadvantages:

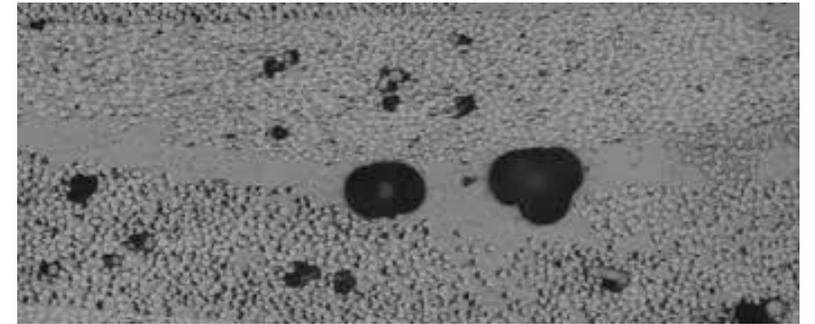
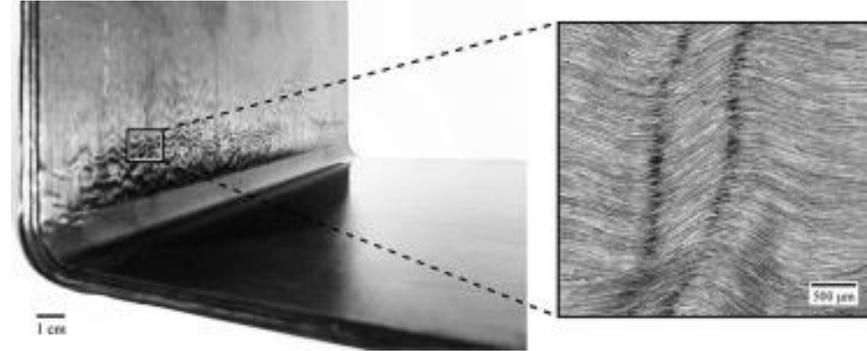
- High Cost
- Low Electrical Conductivity
- Low Thermal Conductivity



Introduction

Defects in composites:

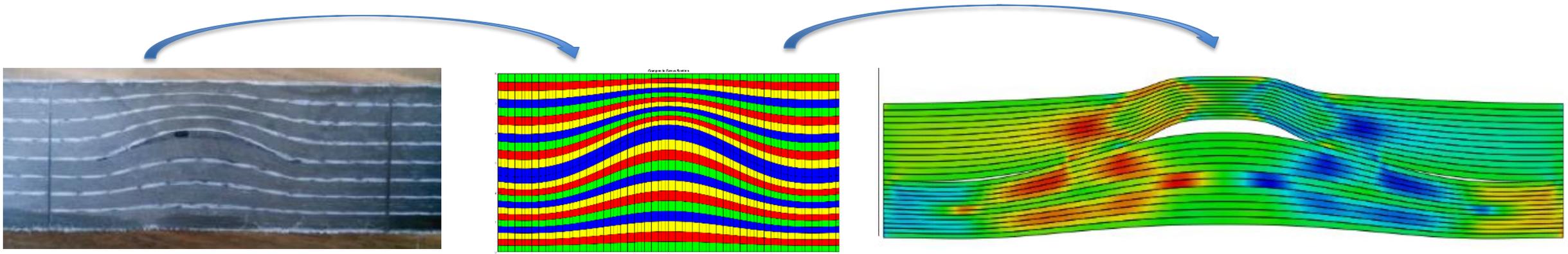
- ✓ Delaminations
- ✓ In-plane fiber waviness
- ✓ Out-of-plane ply wrinkles
- ✓ Foreign Object Damages (FODs)
- ✓ Porosity (Holes)



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Goals

- Developing an automated approach for analyzing wrinkle problems
- Studying the effects of wrinkles on the postbuckling behavior of composites

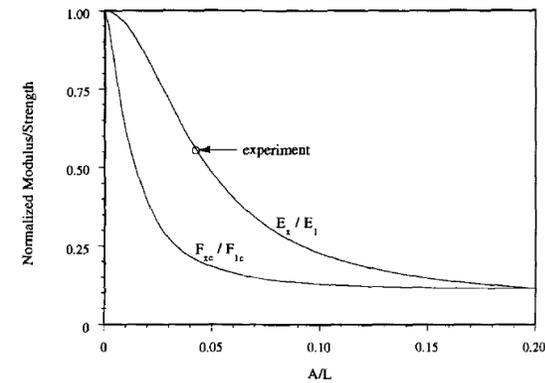
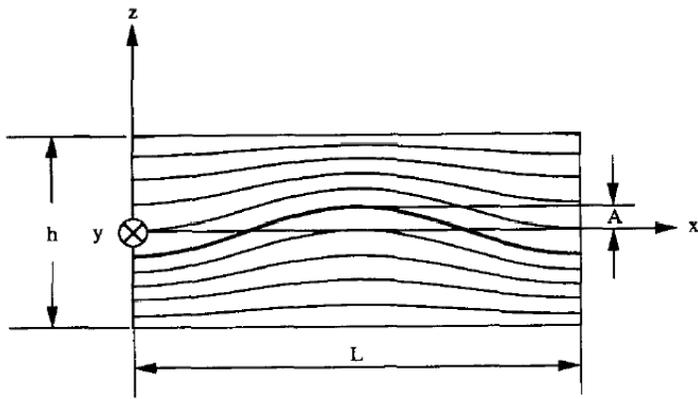


Literature Review



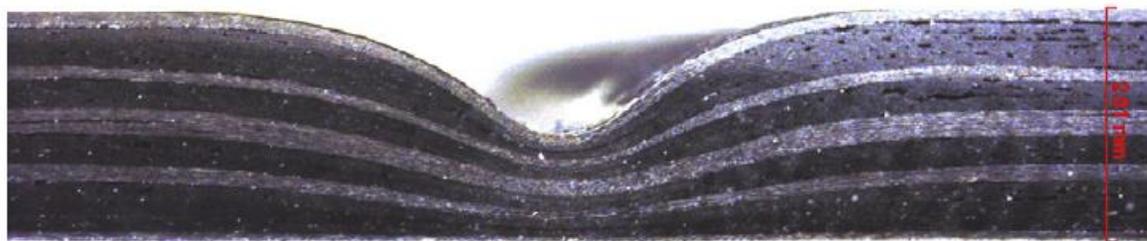
Literature Review

- Hsiao et al. [1,2] used analytical classical laminate theory to find a way for obtaining the effective properties such as Young's modulus and Poisson's ratio. They verified their results by fabricating unidirectional prepreg composites and performing proper mechanical tests.

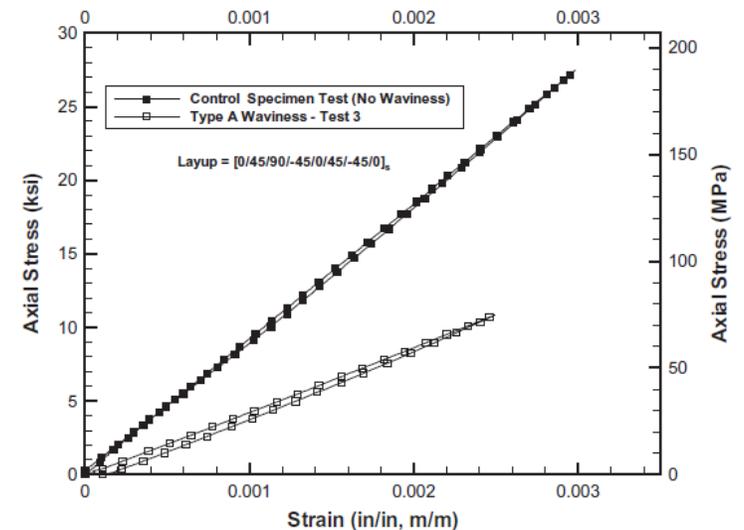


Literature Review

- El-Hajar [3] study presents the results of analytical and experimental efforts performed on the tension behavior of a common aerospace grade carbon fiber/epoxy material system containing out-of-plane fiber waviness. Unidirectional and multidirectional laminates were examined with different thicknesses containing three levels of waviness.

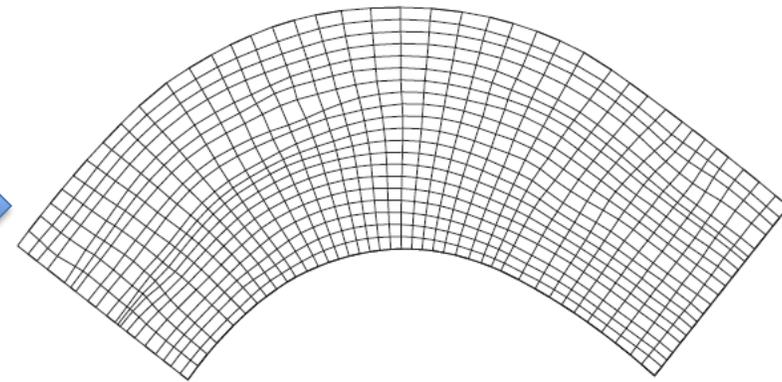
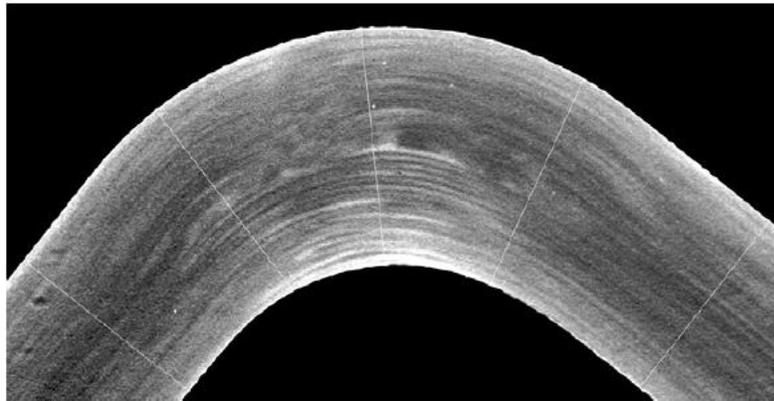


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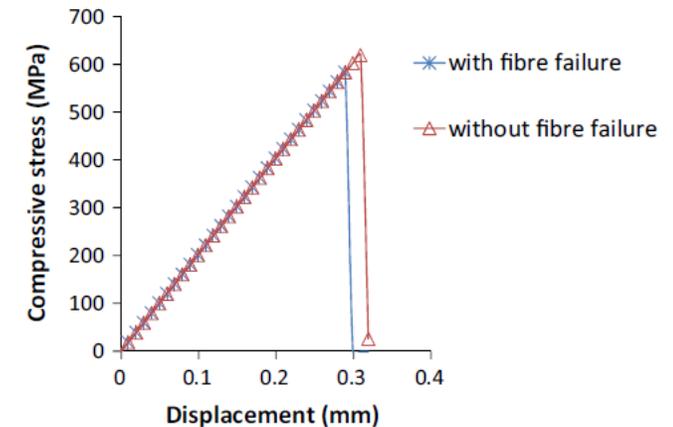
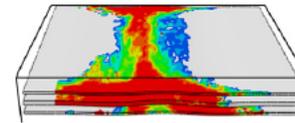
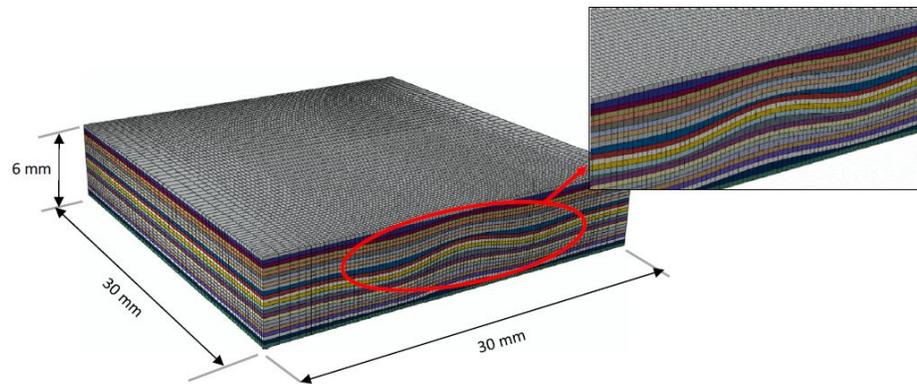
Literature Review

- A method for automated generation of finite element meshes for unidirectional composites with waviness defects is proposed by Nikishkov et al [4]. Images used as input for mesh generation are recorded with X-ray computed micro-tomography.



Literature Review

- An experimental and numerical study has been carried out by Hallet et al. [5] to understand and predict the compressive failure performance of quasi-isotropic carbon–epoxy laminates with out-of-plane wrinkle defects. The wrinkles were seen to significantly reduce the pristine compressive strength of the laminates.



Computational Methodology



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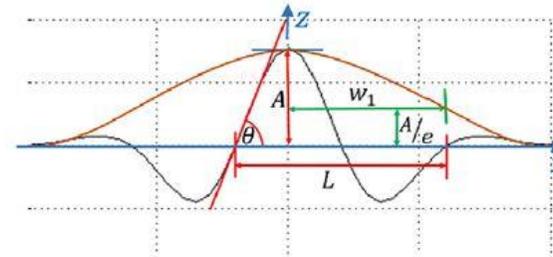
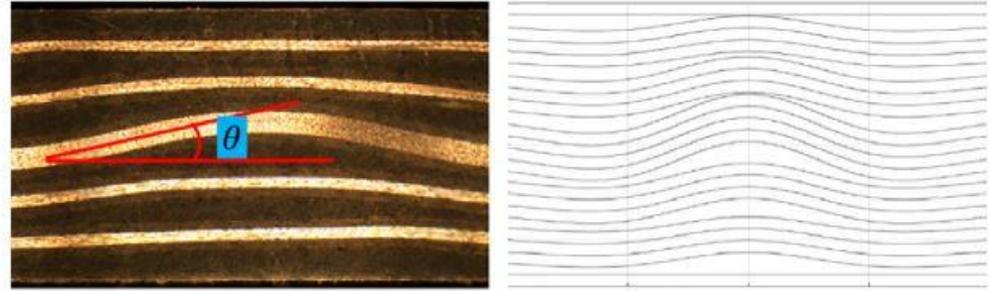


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Problem Definition

✓ The inputs are:

- Number of layers
- Layup orientations
- Location of the wrinkles
- Shape of the wrinkles
- Geometry of the structure



$$d = A_1 e^{-x^2/w_1^2} \cos\left(\frac{2\pi x}{L}\right)$$

Figure 1. Geometry of the problem and wrinkle definition

Automation

```
Main.m x Initial_Calculations.m x Mesh_Generation.m x Making_inp_3D.m x +
1 clear all;close all;fclose all;clc
2 tic
3 %=====
4 %===== Inputs =====
5 LayUp = [45/90/-45/0,3]; SetUp = "sym"; Dimension = "3D"; %OR 2D!
6 Orient = "ON" ;
7 Interface_Elements = "OFF";
8 Interface_Surfaces = "ON" ;
9 CZM = "OFF";
10 Loading = "TensileX"; WrinkleType = "Normal";
11 Thickness = 0.25; Cohesive_Thickness = 0.00;
12 E1 = 161000; E2 = 11380; E3 = E2 ;
13 G12 = 5170; G13 = G12; G23 = 3980;
14 nu12 = 0.32; nu13 = 0.32; nu23 = 0.43;
15
16 nz = 1 ; % Number of elements in each layer in thickness direction
17 Lx = 150; Ly = 25; % Lz = N*th; % Dimensions in X and Y directions
18 ElemX = 200; ElemY = 10; % ElemZ = N*nz;% Numberof elements in X, Y and Z dir
19 %===== Wrinkle Properties =====
20 Amax = 4.0*Thickness;
21 L = 0.4*Lx; W1 = 0.7*Lx; X0 = 0.5*Lx; % X0 is the center of the wave with max amplitude
22 ZFormula = "Linear"; % or gaussian
23 %=====
```

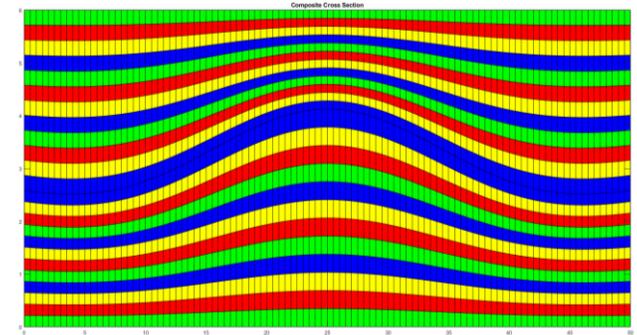
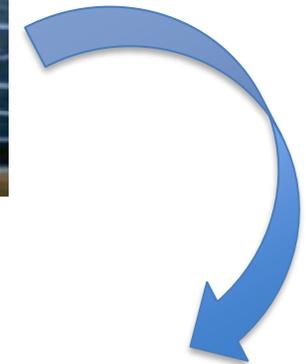


Figure 2. Constructing the FEA mesh



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Zero-thickness cohesive elements

- ✓ No physical gaps between elements
- ✓ Closer to the physics of the problem

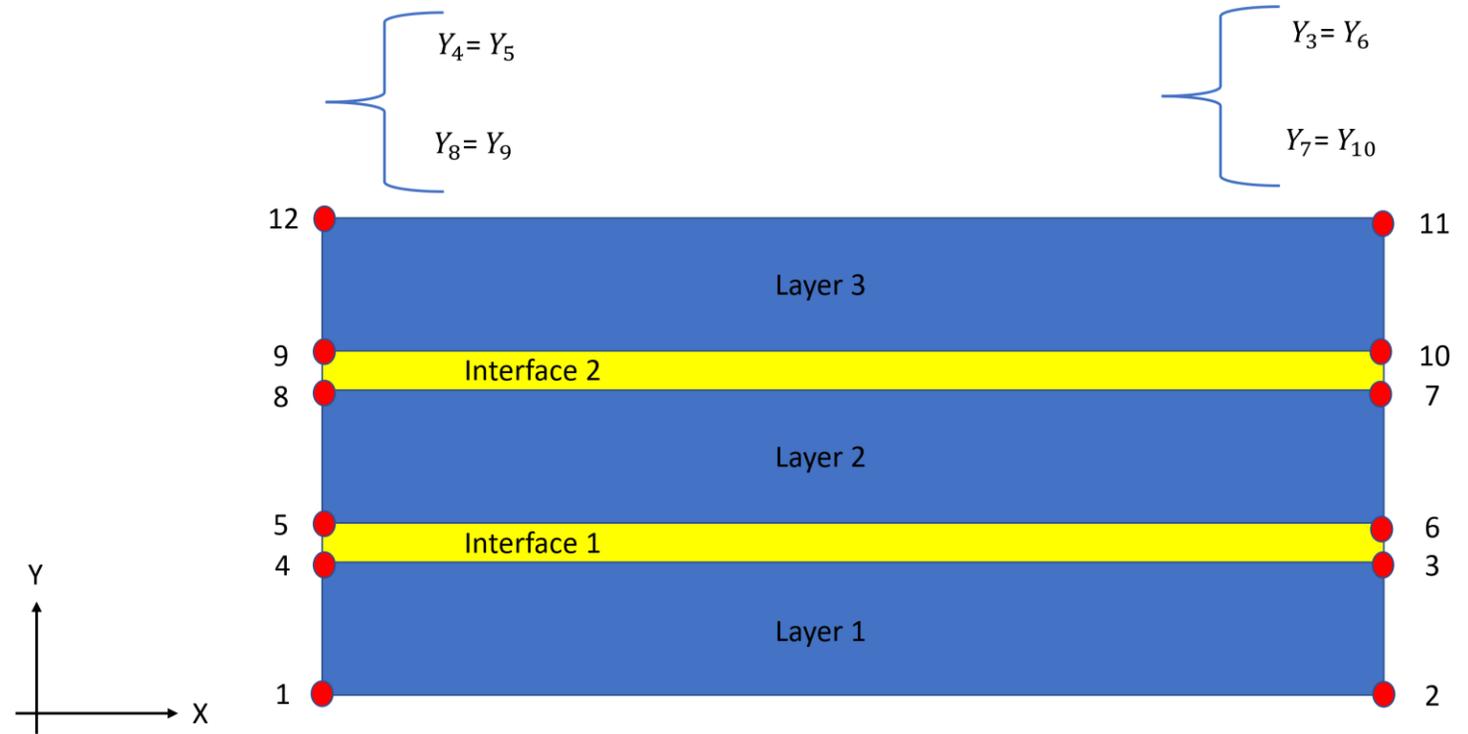


Figure 3. Zero-thickness cohesive elements

Traction-separation law

✓ Material property for cohesive elements

| K_I (N/mm ³) | K_{II} (N/mm ³) | $\sigma_{I\max}$ (MPa) | $\sigma_{II\max}$ (MPa) | G_{Ic} (N/mm) | G_{IIc} (N/mm) | α |
|-------------------------------|----------------------------------|---------------------------|----------------------------|--------------------|---------------------|----------|
| 10^5 | 10^5 | 60 | 90 | 0.26 | 1.002 | 1 |

✓ Damage initiation and progression:

$$f_{mt} = \left(\frac{\sigma_N}{S_T}\right)^2 + \left(\frac{\tau_L}{S_L}\right)^2 + \left(\frac{\tau_T}{S_T}\right)^2 \quad \left(\frac{G_I}{G_{Ic}}\right)^\alpha + \left(\frac{G_{II}}{G_{IIc}}\right)^\alpha = 1$$

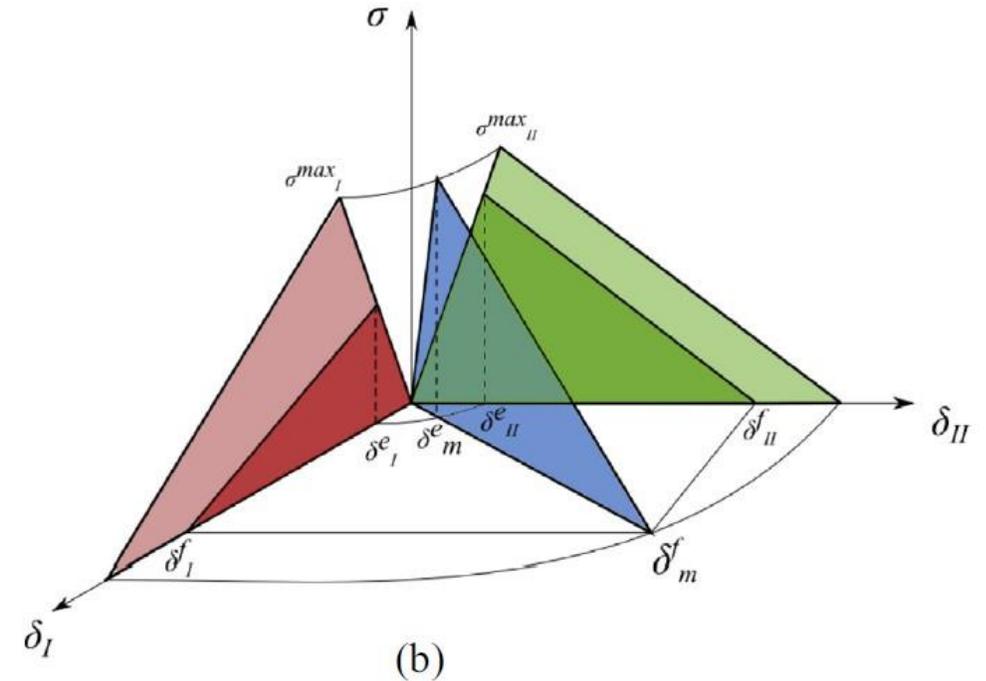
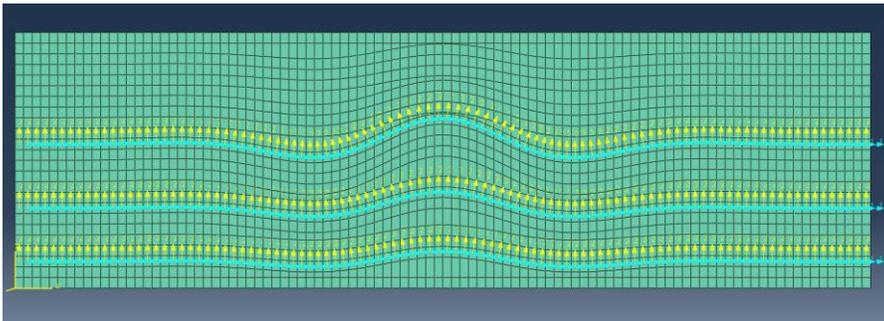


Figure 4. Mixed-mode traction-separation

Abaqus user subroutines

Three Abaqus user subroutines have been developed:

- ✓ UEXTERNALDB
- ✓ ORIENT
- ✓ UMAT



SUBROUTINE UMAT
For all Gauss points

Use the input data from **UEXTERNALDB**
Calculate C_{ijkl} → Calculate the Stresses

End

SUBROUTINE UEXTERNALDB
At the beginning of the analysis (just ONCE!)

Open the file → Read it in → Get what is needed → Pass them to other subroutines.

End

SUBROUTINE ORIENT
For all Elements

Assign a local coordinate to each element.

End

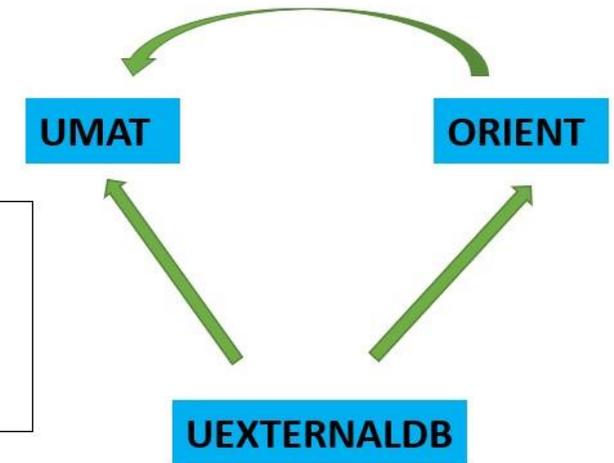


Figure 5. Passing information between Abaqus user subroutines

Postbuckling analysis

Steps for a postbuckling analysis:

1. An Eigenvalue analysis

- Buckling modes (Just a shape!)
- An estimation of buckling loads

2. A large deformation analysis

- Real behavior of the structure
- Delaminations

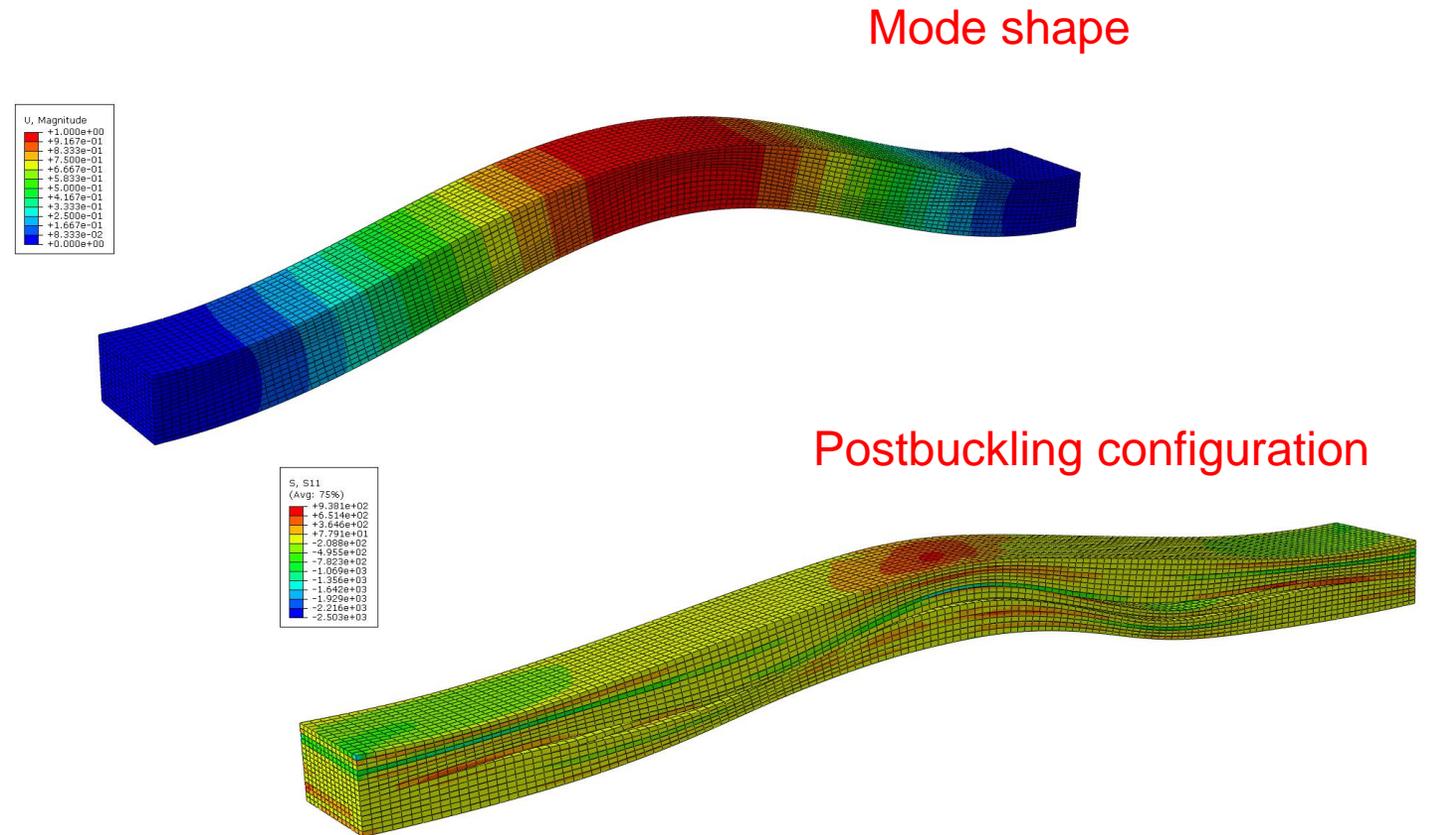


Figure 6. Eigenvalue and postbuckling analysis

Results and Discussion



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Tensile Test:

A 24-layer $[45\backslash 90\backslash -45\backslash 0]_{3S}$ composite under tensile load:

- ✓ S11 axial stress is **12%** higher for the perfect case
- ✓ S13 shear stresses are significantly higher for the wrinkled case

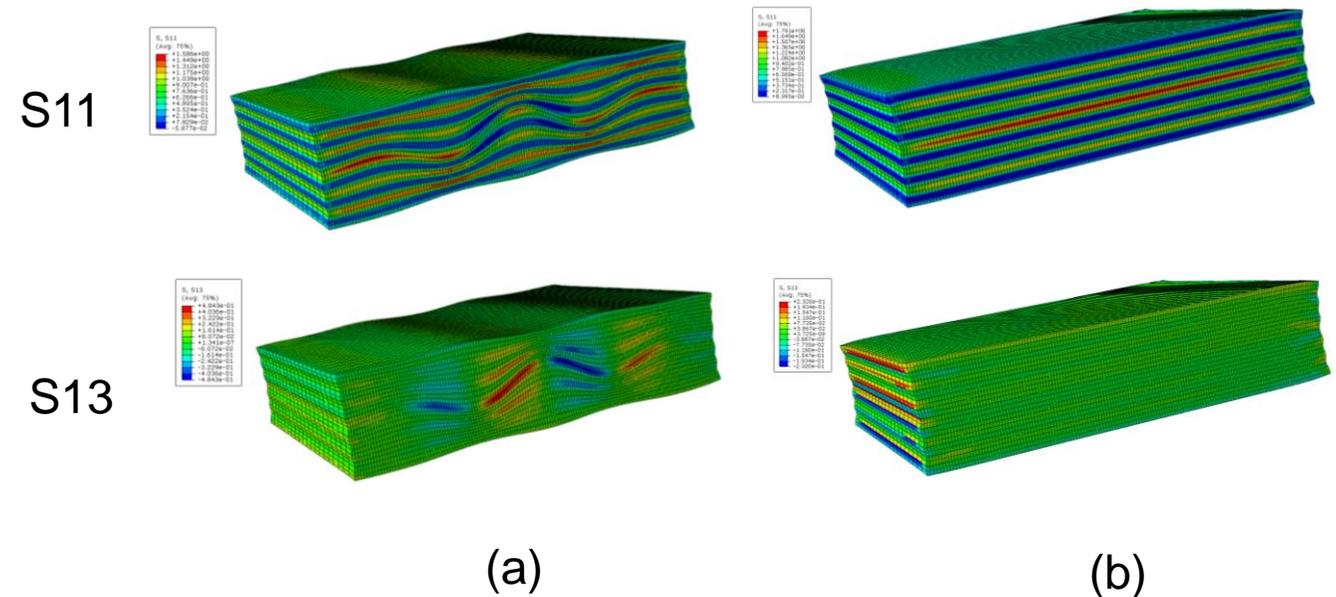


Figure 7. Stress distributions for a (a) wrinkled and (b) perfect composite

Bending Test:

A 24-layer composite $[0]_{24}$ under bending load:

- ✓ Maximum Von Mises stress is 11% higher for the wrinkled composite

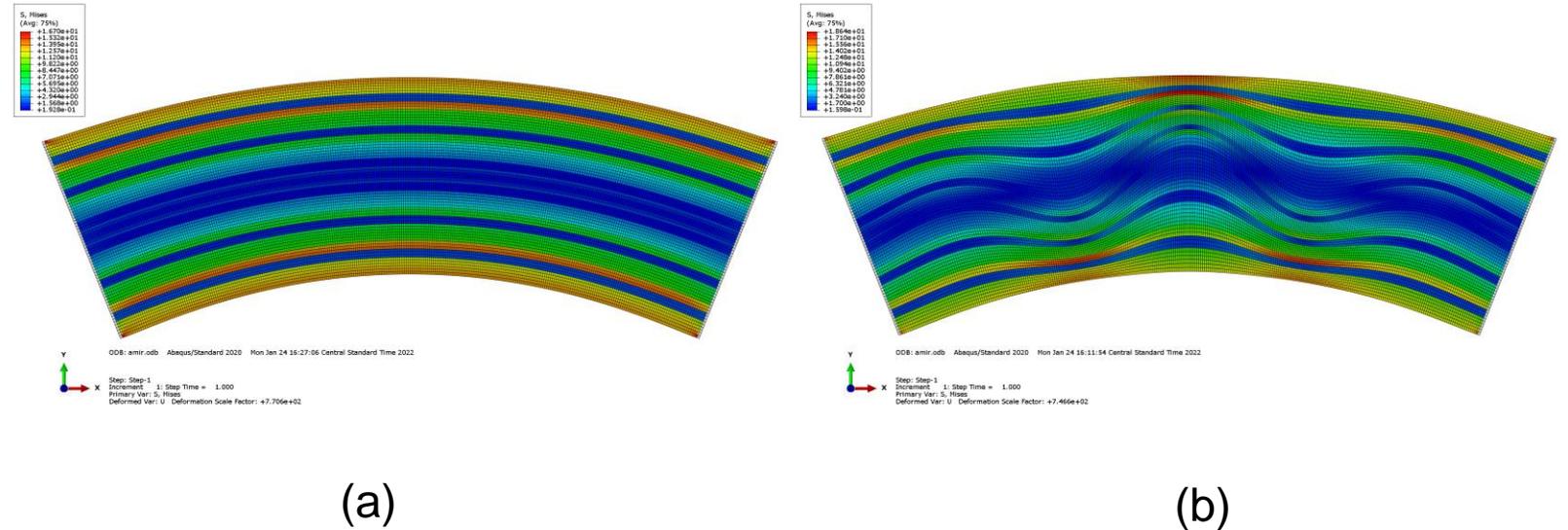


Figure 8. Von Mises stress distributions for a (a) perfect and (b) wrinkled composite

Penetration of elements after fracture:

- ✓ Works reasonably in a simple mode-I fracture

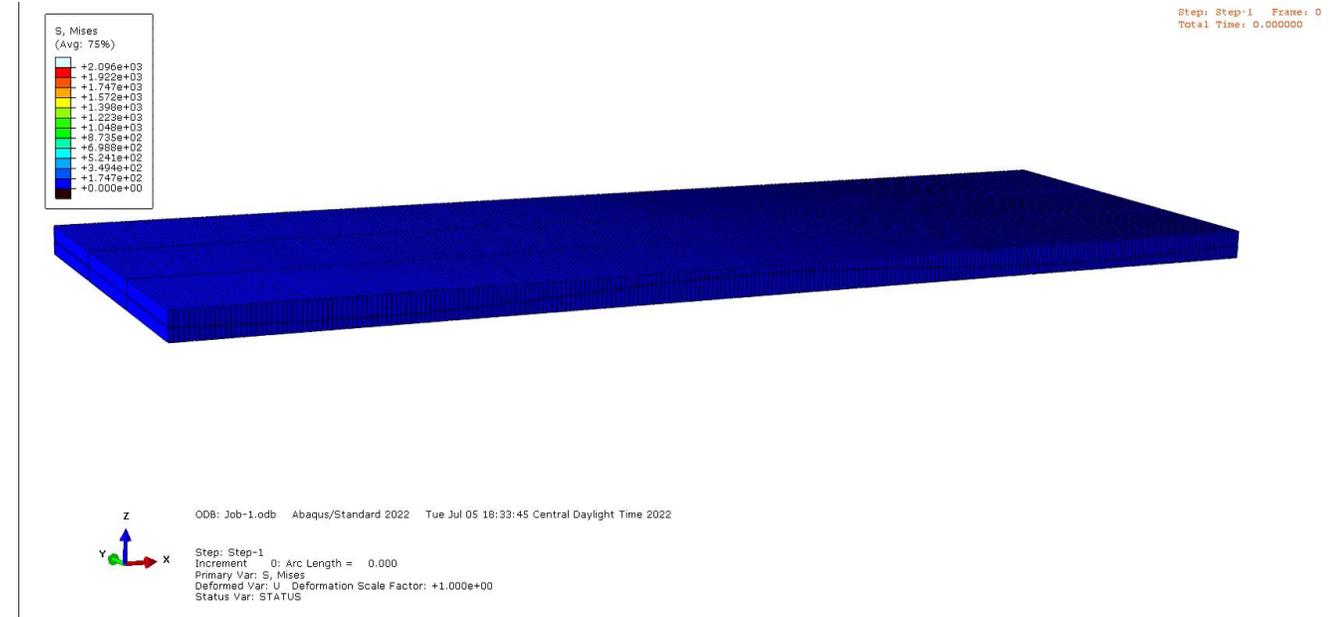
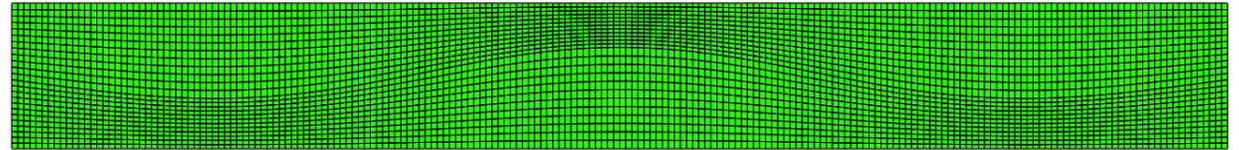
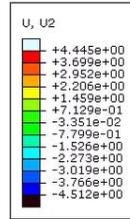


Figure 9. Mode-I fracture in a double cantilever beam test

Penetration of elements after fracture:

- ✓ Prevention of Layers penetration after initial fracture
- ✓ Proper contacts used between every two adjacent layers



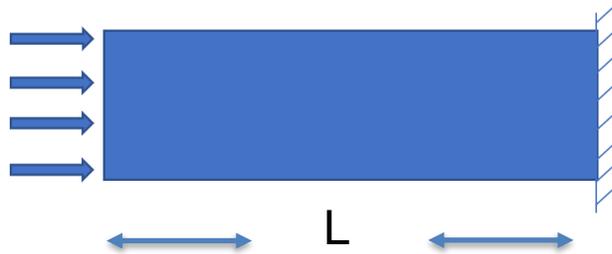
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X
ODB: Job-11658875239.969.odb Abaqus/Standard 2020 Tue Jul 12 08:37:29 Central Daylight Time 2022
Step: Step-1
Increment 0: Step Time = 0.000
Primary Var: U, U2
Deformed Var: U Deformation Scale Factor: +1.000e+00

Figure 10. Von Mises stress distributions for a (a) perfect and (b) wrinkled composite

Postbuckling Analysis:

A series of postbuckling analysis have been performed on the $[0\backslash90]_{6s}$ following composites

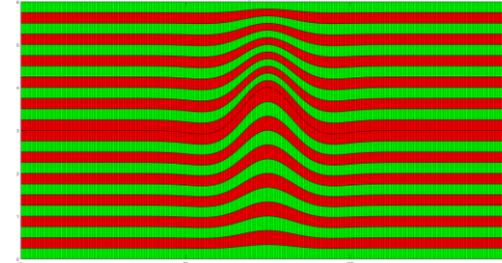
- ✓ Perfect
- ✓ Wide wrinkle
- ✓ Local Wrinkle



(a)



(b)



(c)

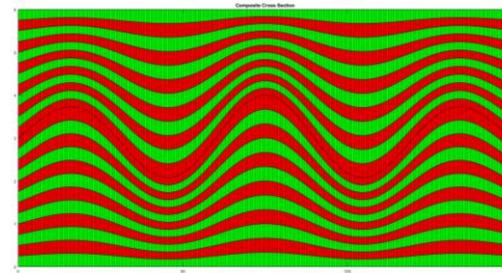


Figure 11. A (a) perfect (b) locally wrinkled (c) widely wrinkled $[0\backslash90]_{6s}$ composite

Postbuckling Analysis:

For a composite with
 $L=100\text{mm}$:

- ✓ 39% reduction of buckling load for locally wrinkled
- ✓ Crack starts to grow right at the wrinkle location
- ✓ 25% reduction of buckling load for widely wrinkled

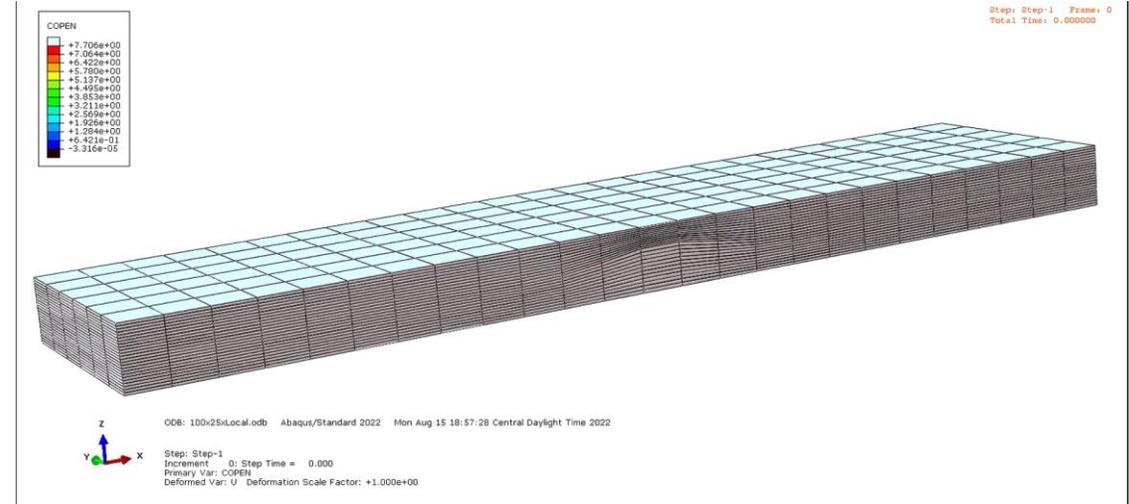
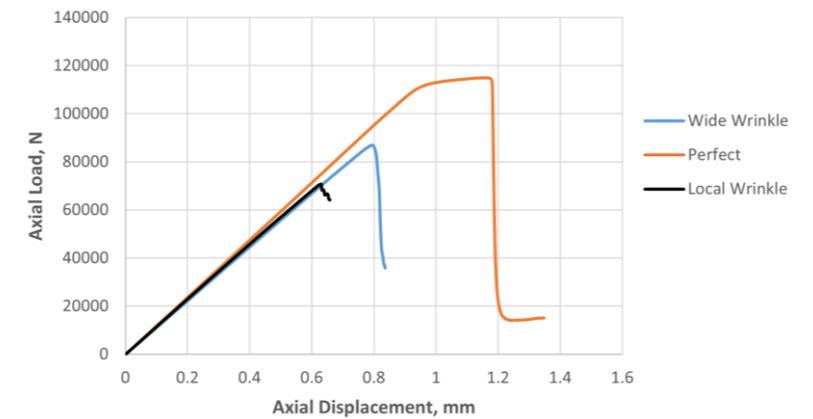


Figure 12. Postbuckling (a) load-displacement plots and (b) behavior of locally wrinkled composite for $L=100\text{mm}$

Postbuckling Analysis:

For a composite with
 $L=130\text{mm}$:

- ✓ **13%** reduction of buckling load for locally wrinkled
- ✓ Load drops are associated with evolution of delamination cracks
- ✓ **7%** reduction of buckling load for widely wrinkled

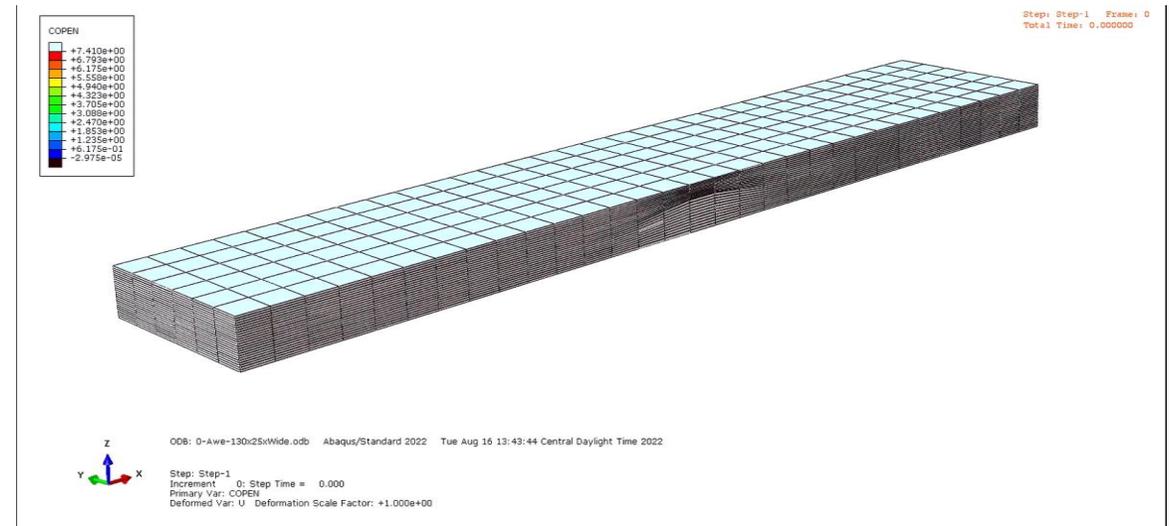
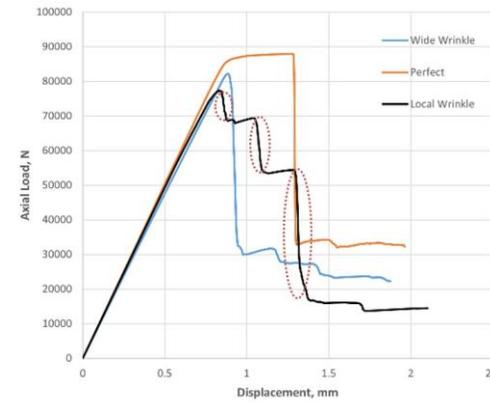


Figure 13. Postbuckling (a) load-displacement plots and (b) behavior of locally wrinkled composite for $L=130\text{mm}$

Postbuckling Analysis:

Effect of the length of the composite (Slenderness)

- ✓ By increasing L , the difference of widely wrinkled and perfect will be diminished (global behavior)
- ✓ Local wrinkles have more detrimental effects

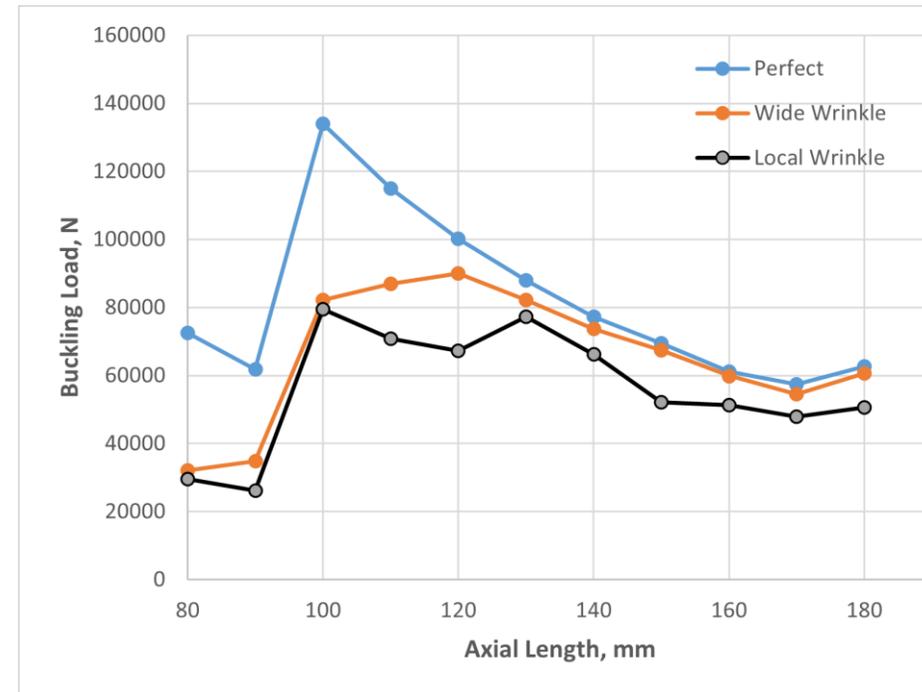


Figure 14. Postbuckling load-displacement plots for different length of the composite

Conclusions



Conclusions and Summary

- ✓ A fully automated MATLAB code has been developed to build the computational model based on the user input geometrical and material properties of the wrinkled problem.
- ✓ Three user subroutines (UEXTERNALDB, ORIENT and UMAT) have been developed for Abaqus simulations.
- ✓ It was observed that presence of wrinkle can considerably affect the shear stresses in a tensile test.
- ✓ Under bending, maximum Von Mises stress for a wrinkled problem was 11% higher than the perfect case with no wrinkle.
- ✓ Zero-thickness elements accompanying with proper contact definitions between the plies can capture the delamination behavior of a composite having wrinkles.
- ✓ It was observed that the presence of wrinkles affect the postbuckling behavior of the composites significantly, up to 40% reduction in buckling loads in some cases.
- ✓ Local wrinkles has more pronounced effects on the postbuckling behavior and delamination growth in the composites.



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References:

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Acknowledgments



Thank You for Your Attention



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Questions?

